

CBSE Class- 9 Important Questions

Chapter – 12

Heron's Formula

Section - A

(1) An isosceles right triangle has an area 8cm^2 . The length of its hypotenuse is

1. $\text{cm } \sqrt{16}$
2. $\text{cm } \sqrt{48}$
3. $\text{cm } \sqrt{32}$
4. $\sqrt{24} \text{ cm}$

Ans. (c) $\sqrt{32} \text{ cm}$

(2) The sides of a triangle are 35 cm, 54 cm, and 61 cm, respectively. The length of its longest altitude is

1. $\text{cm } 26\sqrt{5}$
2. 28 cm
3. $10\text{cm } \sqrt{5}$
4. $24 \sqrt{5} \text{ cm}$

Ans. (d) $24 \sqrt{5} \text{ cm}$

Q.3 The sides of a triangle are 56 cm, 60 cm. and 52 cm. long. The area of the triangle is.

1. 4311 cm^2
2. 4322 cm^2
3. 2392 cm^2
4. None of these

Ans. (d) None of these

Q.4 The area of an equilateral triangle is $16 \sqrt{3} \text{ m}^2$. Its perimeter is



1. 24m
2. 12m
3. 306 m
4. 48m

Ans. (a) 24m

Q.5 The perimeter of a triangle is 30 cm. Its sides are in the ratio 1 : 3 : 2, then its smallest side is.

1. 15 cm
2. 5cm
3. 1 cm
4. 10 cm.

Ans. 5 cm.

Section - B

**Q.6 Find the area of a triangular garden whose sides are 40m., 90m and 70m.
(use $\sqrt{5} = 2.24$)**

Ans. 1344 sq.m.

Q.7 Find the cost of leveling a ground in the form of a triangle with sides 16m, 12m and 20m at Rs. 4 per sq. meter.

Ans. 384

Q.8 Find the area of a triangle, two sides of which are 8cm and 11 cm and the perimeter is 32 cm.

Ans. $8\sqrt{30}$ cm²

Q.9 The area of an isosceles triangle is 12 cm². If one of its equal side is 5cm. Find its base.

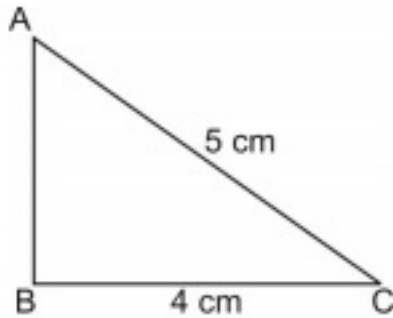
Ans. 6cm.

Q.10 Find the area of a right triangle whose sides containing the right angle are 5cm and 6cm.



Ans. 15 cm^2

Q.11 Find the area of the adjoin figure if $AB \perp BC$



Ans. 6 cm^2

Section - C

Q.12 The diagonals of a rhombus are 24 cm and 10 cm. Find its area and perimeter.

Ans. 120 sq cm . 52 cm .

Q.13 Two side of a parallelogram are 10 cm and 7cm. One of its diagonals is 13 cm. Find the area.

Ans. $40\sqrt{3} \text{ cm}^2$

Q.14 A rhombus shaped sheet with perimeter 40 cm and one diagonal 12 cm, is painted on both sides at the rate of ₹ 5 per m^2 . Find the cost of painting.

Ans. 960

Q.15 The sides of a quadrilateral ABCD are 6cm, 8cm, 12 cm and 14 cm (taken in order) respectively, and the angle between the first two sides is a right angle.

Find its area.

Ans. $24(\sqrt{6} + 1) \text{ cm}^2$

Q.16 The perimeter of an isosceles triangle is 32 cm. The ratio of the equal side to its base is 3 : 2. Find the area of the triangle.

Ans. $32\sqrt{2}$ cm²

Q.17 The sides of a triangular field are 41m, 40m and 9m. Find the number of flower beds that can be prepared in the field, if each flower bed needs 900 cm² space.

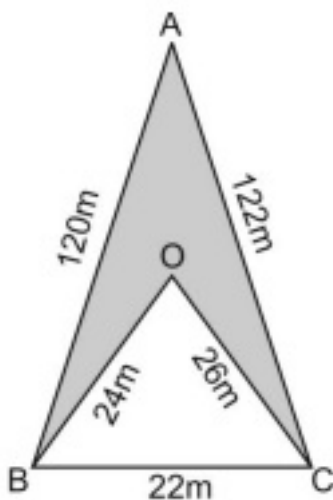
Ans. 2000

Q.18 The perimeter of a triangular ground is 420 m and its sides are in the ratio 6 : 7 : 8. Find the area of the triangular ground.

Ans. $2100\sqrt{15}$ m²

Section - D

Q.19 Calculate the area of the shaded region.



Ans. 1074 m²

Q.20 If each sides of a triangle is double, then find the ratio of area of the new triangle thus formed and the given triangle.

Q.21 A field is in the shape of a trapezium whose parallel sides are 25m and 10m. If its non-parallel sides are 14m and 13m, find its area.

Ans. 196sq.m.

Q.22 An umbrella is made by stitching 10 triangular pieces of cloth of 5 different colour each piece measuring 20 cm, 50 cm and 50 cm. How much cloth of each colour is

required for one umbrella?

($\sqrt{6} = 2.45$)

Ans. 980 cm^2 each.

Q.23 A triangle and a parallelogram have the same base and same area. If the sides of the triangle are 26 cm, 28 cm and 30 cm and the parallelogram stands on the base 28 cm, find the height of the parallelogram.

Ans. 12 cm.



CBSE Class 9 Mathemaics

Important Questions

Chapter 12

Hérons Formula

1 Marks Quetions

1. The measure of each side of an equilateral triangle whose area is $\sqrt{3}$ cm² is

(A) 8 cm

(B) 2 cm

(C) 4 cm

(D) 16 cm

Ans. (B) 2 cm

2. Measure of each side of an equilateral triangle is 12cm. Its area is given by

(A) $9\sqrt{3}$ sq cm

(B) $18\sqrt{3}$ sq cm

(C) $27\sqrt{3}$ sq cm

(D) $36\sqrt{3}$ sq cm

Ans. D) $36\sqrt{3}$ sq cm

3. Two adjacent side of a parallelogram are 74cm and 40cm one of Its diagonals is 102cm. area of the ||gram is

(A) 612 sq m

(B) 1224 sq m

(C) 2448 sq m

(D) 4896 sq m

Ans. (C) 2448 sq m

4.

(B) 8 cm

(C) 6 cm

(D) 5 cm

Ans. (A) 10 cm

5. The perimeter of a triangle is 60cm. If its sides are in the ratio 1:3:2, then its smallest side is

(a) 15

(b) 5

(c) 10

(d) none of these.

Ans. (c) 10

6. The perimeter of a triangle is 36cm. If its sides are in the ratio 1:3:2, then its largest side is

(a) 6

(b) 12

(c) 18

(d) none of these

Ans. (c) 18

7. If the perimeter of a rhombus is 20cm and one of the diagonals is 8cm. The area of the rhombus is

(a) 24 sq cm

(b) 48 sq cm

(c) 50 sq cm

(d) 30 sq cm

Ans. (a) 24 sq cm

8. One of the diagonals of a rhombus is 12cm and area is 54 sq cm. the perimeter of the rhombus is

(a) 72 cm

(b) $\sqrt[3]{10}$ cm

(c) $\sqrt[9]{10}$ cm

(d) $\sqrt[12]{10}$ cm

Ans. (d) $\sqrt[12]{10}$ cm

9. The side of a triangle is 12 cm, 16 cm, and 20 cm. Its area is

(A) 100sq cm

(B) 90sq cm

(C) 96sq cm

(D) 120sq cm.

Ans. (C) 96sq cm

10. The side of an equilateral triangle is $4\sqrt{3}cm$. Its area is.

(A) $12\sqrt{3}$ sq cm

(B) $12\sqrt{6}$ sq cm

(C) $12\sqrt{10}$ sq cm

(D) $6\sqrt{10}$ sq cm.

Ans. (A) $12\sqrt{3}$ sq cm

11. If the perimeter of a rhombus is 20sq cm and one of the diagonals is 8 cm. then the area of the rhombus is

(A) 40sq cm

(B) 24sq cm

(C) 20sq cm

(D) 13sq cm.

Ans. (B) 24sq cm

12. One of the diagonals of a rhombus is 12 cm and Its area is 54sq cm. the perimeter of the rhombus is.

(A) 10 cm

(B) 8 cm

(C) 6 cm

(D) $12\sqrt{10}$ cm.



Ans. (D) $12\sqrt{10}$ cm.

13. The lengths of the side of a triangular park are 90m, 70m and 40m, find Its area.

(A) 1340 sq m

(B) 1344 sq m

(C) 1440 sq m

(D) 1444 sq m

Ans. (B) 1344 sq m

14. An equilateral triangle has a side 50cm long. Find the area of the triangles.

(A) $625\sqrt{3}$ sq cm

(B) $625\sqrt{6}$ sq m

(C) $256\sqrt{6}$ sq m

(D) $625\sqrt{10}$ sq m

Ans. (A) $625\sqrt{3}$ sq cm

15. The area of an isosceles triangle is 12 sq cm. If one of the equal side is 5 cm, then the length of the base is

(A) 4 cm

(B) 5 cm

(C) 6 cm

(D) 8 cm

Ans. (C) 6 cm

16. Find the area of triangle whose side is 6 cm, 10 cm and 15cm.

(A) 404.9 sq cm

(B) 405.9 sq cm

(C) 402.9 sq cm

(D) 410sq cm

Ans. (A) 404.9 sq cm

17. If side of equilateral triangle is 25 m. Its area is

(a) $\frac{625}{4}\sqrt{3}$ sq cm

(b) $54\sqrt{3}$ sq cm

(c) $5\sqrt{3}$ sq cm

(d) $\sqrt{3}$ sq cm

Ans. (a) $\frac{625}{4}\sqrt{3}$ sq cm

18. The perimeter of an equilateral triangle is 48 cm. Its area is

(a) $18\sqrt{3}$ sq cm

(b) $72\sqrt{3}$ sq cm

(c) $64\sqrt{3}$ sq cm

(d) $60\sqrt{3}$ sq cm

Ans. (c) $64\sqrt{3}$ sq cm

19. If area of isosceles triangle is 48 sq cm and length of one of its equal sides is 10 m, then what is the base?

(a) 16 cm or 12 cm

(b) 12 cm or 14 cm

(c) 14 cm or 16 cm

(d) 16 cm or 18 cm

Ans. (a) 16 cm or 12 cm

20. If $AB = 14$ cm, $BC = 13$ cm, $CD = 17$ cm, $DA = 8$ cm and $AC = 15$ cm then area of quadrilateral ABCD is

(a) 150 sq cm

(b) 144 sq cm

(c) 142 sq cm

(d) 140 sq cm

Ans. (b) 144 sq cm



CBSE Class 9 Mathematics

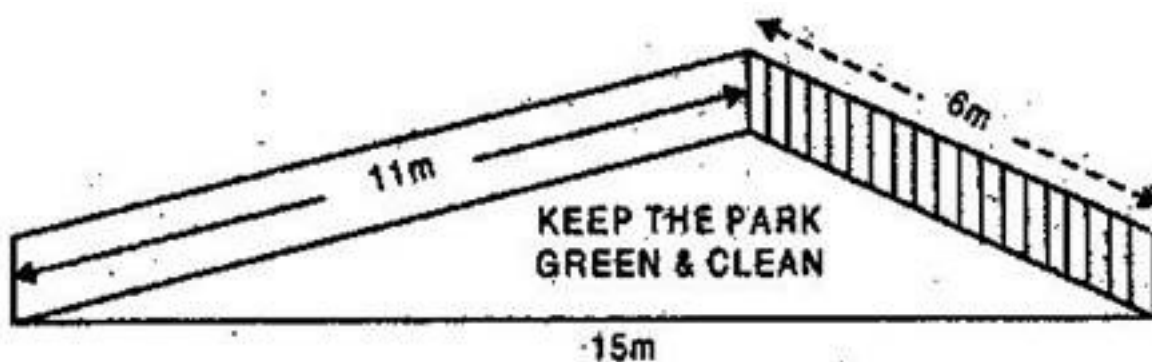
Important Questions

Chapter 12

Heron's Formula

2 Marks Questions

1. There is slide in a park. One of its side walls has been painted in some colour with a message "KEEP THE PARK GREEN AND CLEAN", (see figure). If the sides of the wall are 15 m, 11 m and 6 m, find the area painted in colour.



Ans. Since, sides of coloured triangular wall are 15 m, 11 m and 6 m.

∴ Semi-perimeter of coloured triangular wall

$$= \frac{15+11+6}{2} = \frac{32}{2} = 16 \text{ m}$$

Now, Using Heron's formula,

Area of coloured triangular wall

$$= \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{16(16-15)(16-11)(16-6)}$$

$$= \sqrt{16 \times 1 \times 5 \times 10} = 20\sqrt{2} \text{ m}^2$$

Hence area painted in blue colour = $20\sqrt{2}m^2$

2. Find the area of a triangle two sides of which are 18 cm and 10 cm and the perimeter is 42 cm.

Ans. Given: $a = 18$ cm, $b = 10$ cm.

Since Perimeter = 42 cm

$$\Rightarrow a + b + c = 42$$

$$\Rightarrow 18 + 10 + c = 42$$

$$\Rightarrow c = 42 - 28 = 14 \text{ cm}$$

\therefore Semi-perimeter of triangle

$$= \frac{18+10+14}{2} = 21 \text{ cm}$$

$$\therefore \text{Area of triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{21(21-18)(21-10)(21-14)}$$

$$= \sqrt{21 \times 3 \times 11 \times 7}$$

$$= \sqrt{7 \times 3 \times 3 \times 11 \times 7}$$

$$= 21\sqrt{11}$$

$$= 21 \times 3.3$$

$$= 69.3 \text{ cm}^2$$

3. Sides of a triangle are in the ratio of 12: 17: 25 and its perimeter is 540 cm. Find its area.

Ans. Let the sides of the triangle be $12x, 17x$ and $25x$.

Therefore, $12x + 17x + 15x = 540$

$$\Rightarrow 54x = 540 \Rightarrow x = 10$$

\therefore The sides are 120 cm, 170 cm and 250 cm.

$$\text{Semi-perimeter of triangle } (s) = \frac{120 + 170 + 250}{2} = 270 \text{ cm}$$

$$\text{Now, Area of triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{270(270-120)(270-170)(270-250)}$$

$$= \sqrt{270 \times 150 \times 100 \times 20}$$

$$= 9000 \text{ cm}^2$$

4. An isosceles triangle has perimeter 30 cm and each of the equal sides is 12 cm. Find the area of the triangle.

Ans. Given: $a = 12$ cm, $b = 12$ cm

$$\text{Since Perimeter} = 30 \text{ cm} \Rightarrow a + b + c = 30$$

$$\Rightarrow 12 + 12 + c = 30$$

$$\Rightarrow c = 30 - 24 = 6 \text{ cm}$$

$$\therefore \text{Semi-perimeter of triangle} = \frac{12 + 12 + 6}{2} = 15 \text{ cm}$$

$$\therefore \text{Area of triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

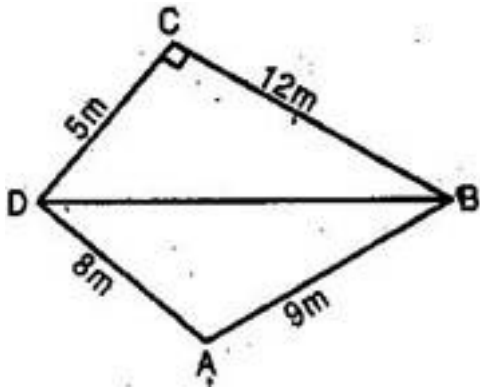
$$= \sqrt{15(15-12)(15-12)(15-6)}$$

$$= \sqrt{15 \times 3 \times 3 \times 9}$$

$$= \sqrt{5 \times 3 \times 3 \times 3 \times 3 \times 3}$$

$$= 9\sqrt{15} \text{ cm}^2$$

5. A park, in the shape of a quadrilateral ABCD has $\angle C = 90^\circ$, AB = 9 m, BC = 12 m, CD = 5 m and AD = 8 m. How much area does it occupy?



Ans. Since BD divides quadrilateral ABCD in two triangles:

(i) Right triangle BCD and (ii) $\triangle ABD$.

In right triangle BCD, right angled at C,

Therefore, Base = CD = 5 m and Altitude = BC = 12 m

$$\therefore \text{Area of } \triangle BCD = \frac{1}{2} \times CD \times BC$$

$$= \frac{1}{2} \times 5 \times 12 = 30 \text{ m}^2$$

In $\triangle ABD$, AB = 9 m, AD = 8 m

And $BD = \sqrt{CD^2 + BC^2}$ [Using Pythagoras theorem]

$$\Rightarrow BD = \sqrt{(5)^2 + (12)^2}$$

$$= \sqrt{25 + 144} = \sqrt{169} = 13 \text{ m}$$

Now, Semi-perimeter of $\triangle ABD = \frac{9 + 8 + 13}{2} = 15 \text{ m}$

Using Heron's formula,

$$\text{Area of } \triangle ABD = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{15(15-9)(15-8)(15-13)}$$

$$= \sqrt{15 \times 6 \times 7 \times 2}$$

$$= 6\sqrt{35} = 6 \times 5.91 \text{ m}^2$$

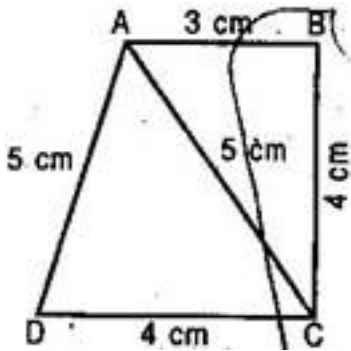
$$= 35.4 \text{ m}^2 \text{ (approx.)}$$

∴ Area of quadrilateral ABCD = Area of $\triangle BCD$ + Area of $\triangle ABD$

$$= 30 + 35.4$$

$$= 65.4 \text{ m}^2$$

6. Find the area of a quadrilateral ABCD in which AB = 3 cm, BC = 4 cm, CD = 4 cm, DA = 5 cm and AC = 5 cm.



Ans. In quadrilateral ABCE, diagonal AC divides it in two triangles, $\triangle ABC$ and $\triangle ADC$.

$$\text{In } \triangle ABC, \text{ Semi-perimeter of } \triangle ABC = \frac{3+4+5}{2} = 6 \text{ cm}$$

Using Heron's formula,

$$\text{Area of } \triangle ABC = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{6(6-3)(6-4)(6-5)}$$

$$= \sqrt{6 \times 3 \times 2 \times 1} = 6 \text{ cm}^2$$

Again, In $\triangle ADC$, Semi-perimeter of $\triangle ADC = \frac{4+5+5}{2} = 7 \text{ cm}$

Using Heron's formula, Area of $\triangle ABC = \sqrt{s(s-a)(s-b)(s-c)}$

$$= \sqrt{7(7-4)(7-5)(7-5)}$$

$$= \sqrt{7 \times 3 \times 2 \times 2} = 2\sqrt{21}$$

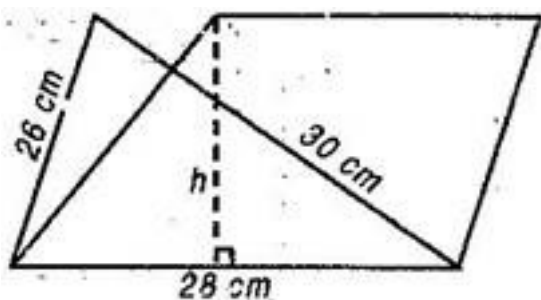
$$= 2 \times 4.6 = 9.2 \text{ cm}^2 \text{ (approx.)}$$

Now area of quadrilateral ABCD = Area of $\triangle ABC$ + Area of $\triangle ADC$

$$= 6 + 9.2$$

$$= 15.2 \text{ cm}^2$$

7. A triangle and a parallelogram have the same base and the same area. If the sides of the triangle are 26 cm, 29 cm and 30 cm and the parallelogram stands on the base 28 cm, find the height of the parallelogram.



Ans. Semi-perimeter of triangle (s) = $\frac{26+28+30}{2} = 42 \text{ cm}$

Using Heron's formula,

$$\begin{aligned} \text{Area of triangle} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{42(42-26)(42-28)(42-30)} \\ &= \sqrt{42 \times 16 \times 14 \times 12} = 336 \text{ cm}^2 \end{aligned}$$

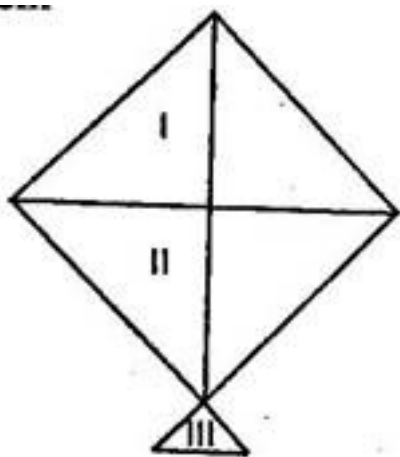
According to question, Area of parallelogram = Area of triangle

$$\Rightarrow \text{Base} \times \text{Corresponding height} = 336$$

$$\Rightarrow 28 \times \text{Height} = 336$$

$$\Rightarrow \text{Height} = 12 \text{ cm}$$

8. A kite is in the shape of a square with a diagonal 32 cm and an isosceles triangle of base 8 cm and sides 6 cm each is to be made of three different shades as shown in figure.



How much paper of each side has been used in it?

Ans. Let ABCD is a square of side a cm and diagonals $AC = BD = 32$ cm

In right triangle ABC, $AB^2 + BC^2 = AC^2$ [Using Pythagoras theorem]

$$\Rightarrow a^2 + a^2 = (32)^2$$

$$\Rightarrow 2a^2 = 32 \times 32$$

$$\Rightarrow a^2 = \frac{32 \times 32}{2} = 512$$

$$\Rightarrow \text{Area of square} = 512 \text{ cm}^2 \text{ [Area of square} = \textit{side} \times \textit{side}]$$

Diagonal BD divides the square in two equal triangular parts I and II.

$$\therefore \text{Area of shaded part I} = \text{Area of shaded part II} = \frac{1}{2} \times 512 = 256 \text{ cm}^2$$

$$\text{Now, semi-perimeter of shaded part III } (s) = \frac{6+6+8}{2} = 10 \text{ cm}$$

$$\text{Area of shaded part III} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{10(10-6)(10-6)(10-8)}$$

$$= \sqrt{10 \times 4 \times 4 \times 2} = 8\sqrt{5}$$

$$= 8 \times 2.236 = 17.88 \text{ cm}^2$$

9. An umbrella is made by stitching 10 triangles pieces of cloth of two different colour, each piece measuring 20 cm 50 cm and 50 cm. How much cloth of each colour is required for the umbrella?

Ans. a=20cm, b=50cm

\therefore cloth required for each colour

$$= 5 \times \text{Area of one triangle piece}$$

$$= 5 \times \frac{a}{4} \sqrt{4b^2 - a^2}$$

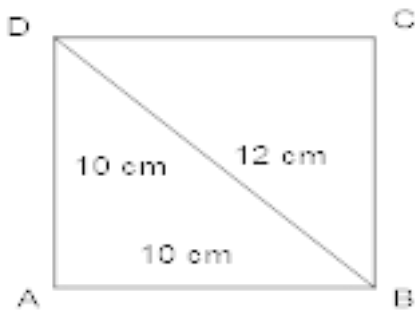
$$= 5 \times \frac{20}{4} \sqrt{4(50)^2 - (20)^2} \text{ sq cm}$$

$$= 25 \times 40\sqrt{6} \text{ sq cm}$$

$$=1000 \times \sqrt{6} \text{ sq cm}$$

Thus, $(1000\sqrt{6})$ sq cm cloth of each colour is required

10. The perimeter of a rhombus ABCD is 40cm. find the area of rhombus of Its diagonals BD measures 12cm



Ans. $\therefore AB = BC = CD = DA = \frac{40}{4} \text{ cm} = 10 \text{ cm}$

now in $\triangle ABD$,

AB=10cm, BD =12cm and DA=10cm

$$\therefore S = \frac{10+12+10}{2} \text{ cm} = 16 \text{ cm}$$

Area of \therefore by herons pormula

$$\triangle ABD = \sqrt{16(16-10)(16-12)(16-10)}$$

$$= \sqrt{16 \times 6 \times 4 \times 6} = 48 \text{ sq cm}$$

$$\therefore \text{area of rhombus ABCD} = 2 \times \text{area of } \triangle ABD$$

$$= 2 \times 48 \text{ sq cm}$$

$$= 96 \text{ sq cm}$$

11. Find area of triangle with two sides as 18cm & 10cm and the perimeter is 42cm.

Ans. Let $a=18$ cm, $b=10$ cm

Perimeter =42cm

$$\therefore a + b + c = 42 \text{ cm}$$

So, $C=14$ cm

$$\therefore S = \frac{a+b+c}{2} = \frac{18+10+14}{2} = 21 \text{ cm}$$

$$\text{new area of triangles} = \sqrt{21(21-18)(21-10)(21-14)}$$

$$= \sqrt{21 \times 3 \times 11 \times 7}$$

$$= 21\sqrt{11} \text{ sq cm}$$

12. Find the area of in isosceles triangle, the measure of one of Its equals side being 'b' and the third side 'a'.

Ans. Here

$$S = \frac{a+b+c}{2} \text{ units} = \frac{a+2b}{2} \text{ units}$$

$$\therefore \text{area of } \Delta = \sqrt{\left(\frac{a+2b}{2}\right)\left(\frac{a+2b}{2}-a\right)\left(\frac{a+2b}{2}-b\right)\left(\frac{a+2b}{2}-c\right)}$$

$$= \sqrt{\left(\frac{a+2b}{2}\right)\left(\frac{2b-a}{2}\right)\frac{a}{2} \times \frac{a}{2}} \text{ sq units}$$

$$= \frac{a}{4} \sqrt{4b^2 - a^2} \text{ sq units}$$

13. Find the cost of leveling the ground in the form of a triangle having its sides are 40 m, 70 m and 90 m at Rs 8 per square meter. [use $\sqrt{5} = 2.24$]



Ans. Here $S = \frac{40+70+90}{2} \text{ m} = 100 \text{ m}$

\therefore Area of a triangular ground = $\sqrt{100(100-40)(100-70)(100-90)} \text{ sq m}$

= $\sqrt{100 \times 60 \times 30 \times 10} \text{ sq m}$

= $(10 \times 10 \times \sqrt[5]{5}) \text{ sq m}$

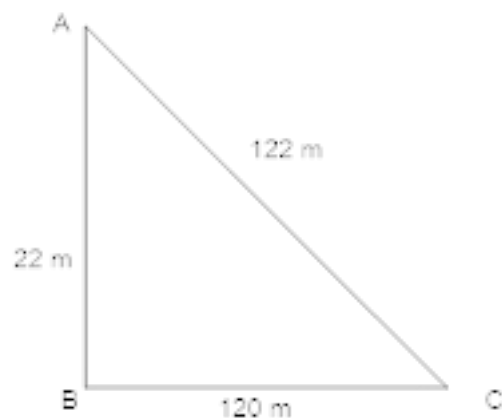
= $(600 \times 2.24) \text{ sq m}$

= 1344 sq m

\therefore Cost of leveling the ground = Rs (8×1344)

=Rs 10752

14. The triangular side's walls of a flyover have been used for advertisements. The sides of the walls are 122m, 22m and 120m. The advertisement yield on earning of Rs 5000 per m^2 per year. A company hired one of its walls for 4 months. How much rent did it pay?



Ans. The lengths of the sides of the walls are 122m, 22m and 120m.

As,

$120^2 + 22^2$

= 14400 + 484

$$= 14884$$

$$= (122)^2$$

∴ Walls are in the form of right triangles

$$\text{Area of one wall} = \frac{1}{2} \times \text{Base} \times \text{height}$$

$$= \frac{1}{2} \times 120 \times 22 \text{ sq m}$$

$$= 1320 \text{ sq m.}$$

$$\text{Rent} = \text{Rs } 5000/\text{sq m per year}$$

∴ Rent for 4 month

$$= \text{Rs } \left[\frac{5000 \times 1320 \times 4}{12} \right]$$

$$= \text{Rs } 22,00,000$$

15. Find the perimeter and area of a triangle whose sides are of length 2cm, 5cm and 5cm.

Ans. Here, $a = 2\text{cm}$, $b = 5\text{cm}$ and $c = 5\text{cm}$

$$\therefore \text{Perimeter} = a + b + c = (2 + 5 + 5) = 12 \text{ cm}$$

$S =$ semi perimeter

$$= \frac{12}{2} = 6 \text{ cm}$$

using Heron's formula,

$$\therefore \text{Area of triangle} = \sqrt{s(s-a)(s-b)(s-c)} \text{ sq cm}$$



$$= \sqrt{6(6-2)(6-5)(6-5)} \text{ sq cm}$$

$$= \sqrt{24} \text{ sq cm}$$

$$= 4.9 \text{ sq cm}$$

16. There is a slide in a park. One of its sides wall has been painted in some colour with a message “KEEP THE CITY GREEN AND CLEAN”.

If the sides of the wall are 15m, 11m and 6m. Find the area painted in colour.

Ans. ∴ The sides of the wall is in the triangular form with sides,

$$A = 15 \text{ m, } b = 6 \text{ m and } c = 11 \text{ m}$$

$$\therefore S = \frac{15+6+11}{2} \text{ m}$$

$$= 16 \text{ m}$$

∴ Area to be painted in colour = Area of the side wall

$$= \sqrt{s(s-a)(s-b)(s-c)} \text{ sq cm}$$

$$= \sqrt{16(16-5)(16-6)(16-11)} \text{ sq m}$$

$$= \sqrt[4]{50} \text{ sq m}$$

$$= \sqrt[20]{2} \text{ sq m}$$

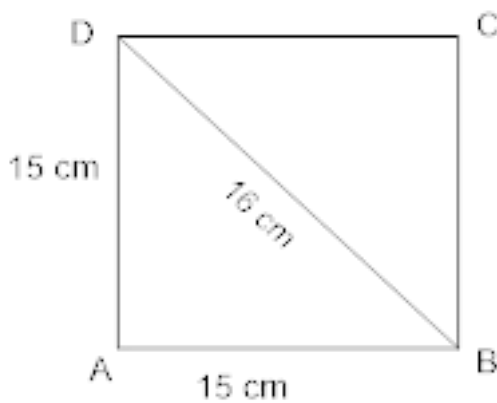
17. Find the area of isosceles triangle whose side is 14 m, 12 m, 14m?

$$\text{Ans. } S = \frac{14+12+14}{2} = 20 \text{ m}$$

$$\text{Area of isosceles triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$\begin{aligned}
&= \sqrt{20(20-14)(20-12)(20-14)} \\
&= \sqrt{20 \times 6 \times 8 \times 6} \\
&= 6\sqrt{160} = 6 \times 12.6 \\
&= 75.6
\end{aligned}$$

18. The perimeter of a rhombus ABCD is 60 cm. find the area of the rhombus if its diagonal BD measures 16 cm?



Ans. As side of rhombus are equal.

$$\therefore AB = BC = CD = DA = \frac{60}{4} = 15 \text{ cm}$$

in ΔABD ,

$$S = \frac{15 + 15 + 16}{2} = 23 \text{ cm}$$

So,

$$\begin{aligned}
\text{Area of } \Delta ABD &= \sqrt{23(23-15)(23-15)(23-16)} \\
&= \sqrt{23 \times 8 \times 8 \times 7} = 8\sqrt{23 \times 7}
\end{aligned}$$

$$= 8 \times 12.7 = 101.6 \text{ sq cm}$$

$$\text{Area of rhombus} = 2 \times 101.6 = 203.2 \text{ sq cm}$$

19. Find the cost of leveling the ground in the form of a triangle having its sides as 70 cm, 50 cm, and 60 cm, at Rs 7 per square meter.

$$\text{Ans. } s = \frac{70 + 50 + 60}{2} = \frac{180}{2} = 90 \text{ cm}$$

$$\therefore \text{ area of triangle} = \sqrt{90(90 - 70)(90 - 50)(90 - 60)}$$

$$= \sqrt{90 \times 20 \times 40 \times 30}$$

$$= 1469.7 \text{ sq m}$$

$$\therefore \text{ cost of levelling the ground} = \text{RS } (7 \times 1469.7)$$

$$= 10287.9$$

20. Find the area of a triangle two sides of the triangle are 18 cm, and 12 cm. and the perimeter is 40 cm.

$$\text{Ans. Let } a=18 \text{ cm, } b=12 \text{ cm and } C=?$$

$$\text{So, } a+b+c=40 \text{ cm}$$

$$18+12+C=40$$

$$C=(40-30) \text{ cm} = 10 \text{ cm}$$

$$\therefore s = \frac{18+12+10}{2} = 20 \text{ cm}$$

$$\therefore \text{ area of triangle} = \sqrt{20(20-18)(20-12)(20-10)}$$

$$= \sqrt{20 \times 2 \times 8 \times 10} \text{ sq cm}$$

$$=56.56 \text{ sq cm}$$

21. Find the area of triangle whose side is 42m, 56m and 70m?

$$\text{Ans. } s = \frac{42+56+70}{2} \text{ m} = \frac{168}{2} \text{ m or } 84$$

$$\therefore \text{Area of } \triangle ABC = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{84(84-42)(84-56)(84-70)} \text{ sq m}$$

$$= 42 \times 28 \text{ sq m}$$

$$= 1176 \text{ sq m}$$

22. Find the area of an isosceles triangle, the measure of one of its equal side being b and the third side a .

$$\text{Ans. } s = \frac{a+b+b}{2} \text{ units} = \frac{a+2b}{2} \text{ units}$$

$$\therefore \text{Area of triangle} = \sqrt{\frac{a+2b}{2} \times \left(\frac{a+2b}{2} - a\right) \left(\frac{a+2b}{2} - a\right) \left(\frac{a+2b}{2} - a\right)} \text{ units}$$

$$= \sqrt{\left(\frac{a+2b}{2}\right) \times \left(\frac{2b-a}{2}\right) \times \frac{a}{2} \times \frac{a}{2}} \text{ units}$$

$$= \frac{a}{4} \sqrt{4b^2 - a^2} \text{ sq units}$$

23. Find the area of equilateral triangle whose side is 12 cm using Heron's formula.

$$\text{Ans. } s = \frac{12+12+12}{2} \text{ cm}$$



$$= \frac{36}{2} \text{ cm} = 18 \text{ cm}$$

$$\therefore \text{Area of equilateral} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{18(18-12)(18-12)(18-12)}$$

$$= \sqrt{18 \times 6 \times 6 \times 6}$$

$$= 36\sqrt{3} \text{ sq cm}$$

24. Find the area of isosceles triangle whose equal side is 6 cm, 6 cm and 8 cm.

$$\text{Ans. } s = \frac{6+6+8}{2} \text{ cm}$$

$$= \frac{20}{2} = 10 \text{ cm}$$

$$\therefore \text{Area of isosceles triangle} = \sqrt{10(10-6)(10-6)(10-8)}$$

$$= \sqrt{10 \times 4 \times 4 \times 2} \text{ sq cm}$$

$$= 17.8 \text{ sq cm}$$

25. Find the area of an isosceles triangles, the measure of one of its equal sides being 10 cm and the third side is 6 cm.

$$\text{Ans. } s = \frac{10+10+6}{2} = \frac{26}{2} = 13 \text{ cm}$$

$$\therefore \text{Area of triangle} = \sqrt{13(13-5)(13-5)(13-6)} \text{ sq cm}$$

$$= \sqrt{13 \times 3 \times 3 \times 7} \text{ sq cm}$$

$$= 3\sqrt{91} \text{ sq cm}$$



26. Find the area of equilateral triangle the length of one of its sides being 24 cm.

Ans. $a = b = c = 24$ cm

$$\therefore S = \frac{24 + 24 + 24}{2} \text{ cm} = \frac{72}{2} \text{ cm}$$

=36 cm

$$\therefore \text{Area of triangle} = \sqrt{36(36-24)(36-24)(36-24)} \text{ sq cm}$$

=246.12 sq cm

27. Find the perimeter and area of a triangle whose sides are 3 cm, 4 cm and 10 cm?

Ans. Perimeter = $3+4+5$

= 12 cm

$$\therefore S = \text{semiperimeter} = \frac{12}{2}$$

Or = 6cm

$$\text{Area of triangle} = \sqrt{6(6-3)(6-4)(6-5)} \text{ sq cm}$$

= 6 sq cm

28. Using Heron's formula, find area of triangle whose sides are 6 cm, 8 cm and 10 cm?

$$\text{Ans. } S = \frac{6+8+10}{2} = \frac{24}{2}$$

=12 cm

$$\therefore \text{Area of triangle} = \sqrt{12(12-6)(12-8)(12-10)} \text{ sq cm}$$

=24 sq cm

CBSE Class 9 Mathematics

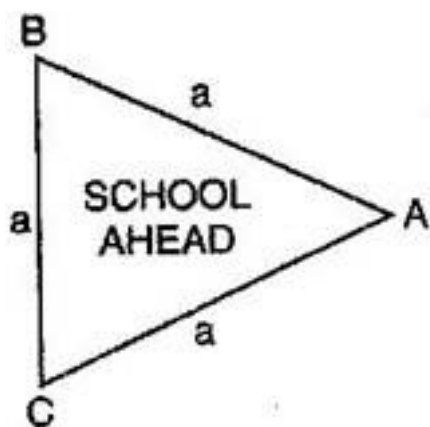
Important Questions

Chapter 12

Heron's Formula

3 Marks Questions

1. A traffic signal board, indicating 'SCHOOL AHEAD' is an equilateral triangle with side 'a'. Find the area of the signal board, using Heron's formula. If its perimeter is 180 cm, what will be the area of the signal board?



Ans. Let the Traffic signal board is $\triangle ABC$.

According to question, Semi-perimeter of $\triangle ABC$ (s) = $\frac{a+a+a}{2} = \frac{3a}{2}$

Using Heron's Formula, Area of triangle ABC = $\sqrt{s(s-a)(s-b)(s-c)}$

$$= \sqrt{\frac{3a}{2} \left(\frac{3a}{2} - a \right) \left(\frac{3a}{2} - a \right) \left(\frac{3a}{2} - a \right)}$$

$$= \sqrt{\frac{3a}{2} \times \frac{a}{2} \times \frac{a}{2} \times \frac{a}{2}} = \sqrt{3 \left(\frac{a}{2} \right)^4}$$

$$= \frac{\sqrt{3}a^2}{4}$$



Now, Perimeter of this triangle = 180 cm

$$\Rightarrow \text{Side of triangle } (a) = \frac{180}{3} = 60 \text{ cm}$$

$$\Rightarrow \text{Semi-perimeter of this triangle} = \frac{180}{2} = 90 \text{ cm}$$

Using Heron's Formula, Area of this triangle = $\sqrt{s(s-a)(s-b)(s-c)}$

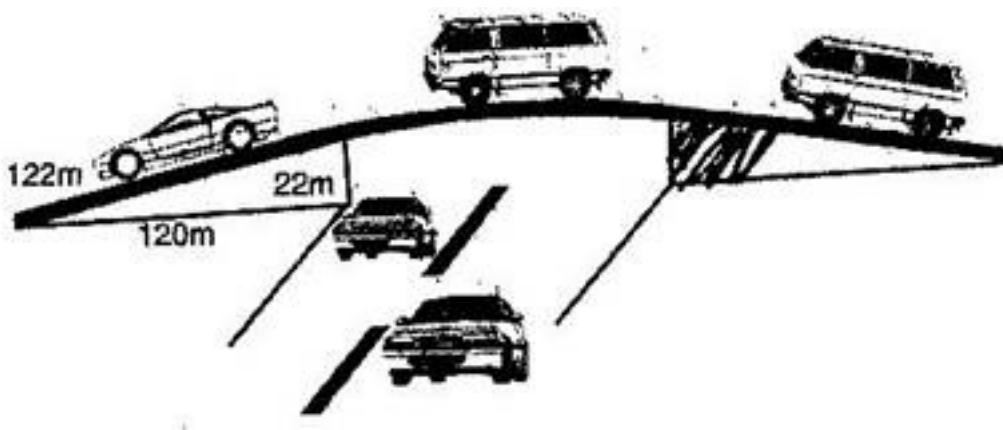
$$= \sqrt{90(90-60)(90-60)(90-60)}$$

$$= \sqrt{90 \times 30 \times 30 \times 30}$$

$$= 30 \times 30 \sqrt{3}$$

$$= 900\sqrt{3} \text{ cm}^2$$

2. The triangular side walls of a flyover has been used for advertisements. The sides of the walls are 122 m, 22 m and 120 m (see figure). The advertisement yield an earning of Rs. 5000 per m^2 per year. A company hired one of its walls for 3 months, how much rent did it pay?



Ans. Given: $a = 122 \text{ m}$, $b = 22 \text{ m}$ and $c = 120 \text{ m}$

$$\text{Semi-perimeter of triangle } (s) = \frac{122+22+120}{2} = \frac{264}{2} = 132 \text{ m}$$



Using Heron's Formula,

$$\begin{aligned}\text{Area of triangle} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{132(122-132)(132-22)(132-120)} \\ &= \sqrt{132 \times 10 \times 110 \times 12} \\ &= \sqrt{11 \times 12 \times 10 \times 10 \times 11 \times 12} \\ &= 10 \times 11 \times 12 \\ &= 1320 \text{ m}^2\end{aligned}$$

\therefore Rent for advertisement on wall for 1 year = Rs. 5000 per m^2

$$\therefore \text{Rent for advertisement on wall for 3 months for } 1320 \text{ m}^2 = \frac{5000}{12} \times 3 \times 1320$$

$$= \text{Rs. } 1650000$$

Hence rent paid by company = Rs. 16,50,000

3. Radha made a picture of an aeroplane with coloured paper as shown in figure. Find the total area of the paper used.

Ans. Area of triangular part I: Here, Semi-perimeter (s) = $\frac{5+5+1}{2} = 5.5$ cm

$$\begin{aligned}\text{Therefore, Area} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{5.5(5.5-5)(5.5-5)(5.5-1)} \\ &= \sqrt{5.5 \times 0.5 \times 0.5 \times 4.5} = 0.75\sqrt{11} \\ &= 0.75 \times 3.31 = 2.4825 \text{ cm}^2\end{aligned}$$

Area of triangular part II = *Length* × *Breadth*

$$= 6.5 \times 1 = 6.5 \text{ cm}^2$$

Area of triangular part III (trapezium): $\frac{1}{2}(AB + DC) \times AE$

$$= \frac{1}{2} (AB + DC) \times \sqrt{AD^2 - DE^2}$$

$$= \frac{1}{2} (1 + 2) \times \sqrt{1 - .025}$$

$$= \frac{1}{2} \times 3 \times \frac{\sqrt{3}}{2}$$

$$= \frac{3 \times 1.732}{4}$$

$$= 1.299 \text{ cm}^2$$

Area of triangular parts IV & V: $2 \left(\frac{1}{2} \times 1.5 \times 6 \right)$

$$= 9 \text{ cm}^2$$

$$\therefore \text{Total area} = 2.4825 + 6.2 + 1.299 + 9$$

$$= 19.28 \text{ cm}^2$$

4. A rhombus shaped field has green grass for 18 cows to graze. If each side of the rhombus is 30 m and its longer diagonal is 48 m, grass of how much area of grass field will each cow be getting?

Ans. Here, $AB = BC = CD = DA = 30$ m and Diagonal $AC = 48$ m which divides the rhombus ABCD in two congruent triangle.

$$\therefore \text{Area of } \triangle ABC = \text{Area of } \triangle ACD$$

Now, Semi-perimeter of $\triangle ABC$ (s) = $\frac{30+30+48}{2} = 54$ m

Now Area of rhombus ABCD = Area of $\triangle ABC$ + Area of $\triangle ACD$

= 2 x Area of $\triangle ABC$ [\because Area of $\triangle ABC$ = Area of $\triangle ACD$]

= $2\sqrt{s(s-a)(s-b)(s-c)}$ [Using Heron's formula]

= $2 \times \sqrt{54(54-30)(54-30)(54-48)}$

= $2 \times \sqrt{54 \times 24 \times 24 \times 6} = 2 \times 6 \times 24$

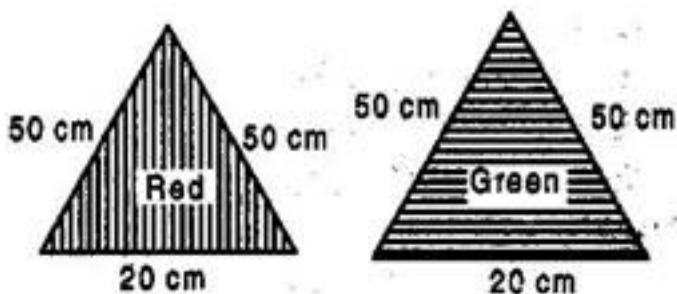
= 864 m^2

\therefore Field available for 18 cows to graze the grass = 864 m^2

\therefore Field available for 1 cow to graze the grass = $\frac{864}{18} = 48 \text{ m}^2$

5. An umbrella is made by stitching 10 triangular pieces of cloth of two different colours (see figure), each piece measuring 20 cm, 50 cm and 50 cm. How much cloth of each colour is required for the umbrella?

Ans. Here, sides of each of 10 triangular pieces of two different colours are 20 cm, 50 cm and 50 cm.



Semi-perimeter of each triangle (s) = $\frac{20+50+50}{2} = 60$ cm

$$\text{Now, Area of each triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{60(60-20)(60-50)(60-50)}$$

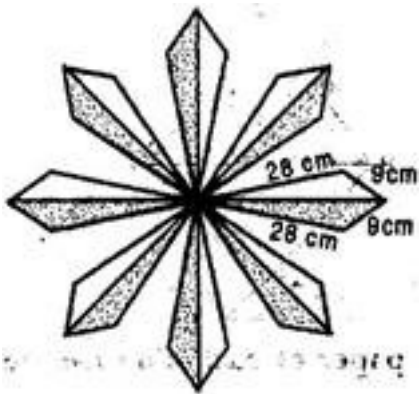
$$= \sqrt{60 \times 40 \times 10 \times 10} = 200\sqrt{6} \text{ cm}^2$$

According to question, there are 5 pieces of red colour and 5 pieces of green colour.

$$\therefore \text{Cloth required for 5 red pieces} = 5 \times 200\sqrt{6} = 1000\sqrt{6} \text{ cm}^2$$

$$\text{And Cloth required to 5 green pieces} = 5 \times 200\sqrt{6} = 1000\sqrt{6} \text{ cm}^2$$

6. A floral design on a floor is made up of 16 tiles which are triangular, the sides of the triangle being 9 cm, 28 cm and 35 cm (see figure). Find the cost of polishing the tiles at the rate of 50 paise per cm^2 .



Ans. Here, Sides of a triangular shaped tile are 9 cm, 28 cm and 35 cm.

$$\text{Semi-perimeter of tile } (s) = \frac{9+28+35}{2} = 36 \text{ cm}$$

$$\text{Area of triangular shaped tile} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{36(36-9)(36-28)(36-35)}$$

$$= \sqrt{36 \times 27 \times 8 \times 1} = 36\sqrt{6}$$

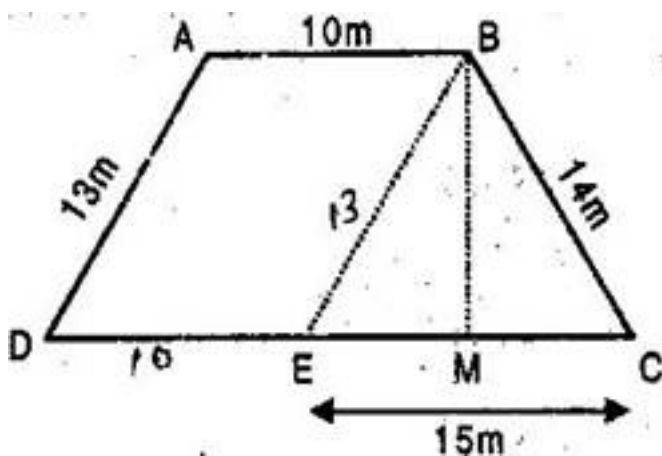
$$= 36 \times 2.45 = 88.2 \text{ cm}^2 \text{ (approx.)}$$

$$\therefore \text{Area of 16 such tiles} = 16 \times 88.2 = 1411.2 \text{ cm}^2 \text{ (Approx.)}$$

$$\therefore \text{Cost of polishing } 1 \text{ cm}^2 \text{ of tile} = \text{Rs. } 0.50$$

$$\therefore \text{Cost of polishing } 1411.2 \text{ cm}^2 \text{ of tile} = \text{Rs. } 0.50 \times 1411.2 = \text{Rs. } 705.60 \text{ (Approx.)}$$

7. A field is in the shape of a trapezium whose parallel sides are 25 m and 10 m. The non-parallel sides are 14 m and 13 m. Find the area of the field.



Ans. Let ABCD be a field in the shape of trapezium and parallel side $AB = 10 \text{ m}$ & $CD = 25 \text{ m}$

And Non-parallel sides $AD = 13 \text{ m}$ and $BC = 14 \text{ m}$

Draw $BM \perp DC$ and $BE \parallel AD$ so that ABED is a parallelogram.

$$\therefore BE = AD = 13 \text{ m and } DE = AB = 10 \text{ m}$$

$$\text{Now in } \triangle BEC, \text{ Semi-perimeter } (s) = \frac{13 + 14 + 15}{2}$$

$$= 21 \text{ m}$$

$$\text{Area of } \triangle BEC = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{21(21-13)(21-14)(21-15)}$$

$$= \sqrt{21 \times 8 \times 7 \times 6} = 84 \text{ m}^2$$

And Area of Δ BEC = 84 m^2

$$\Rightarrow \frac{1}{2} \times EC \times BM = 84$$

$$\Rightarrow \frac{1}{2} \times 15 \times BM = 84$$

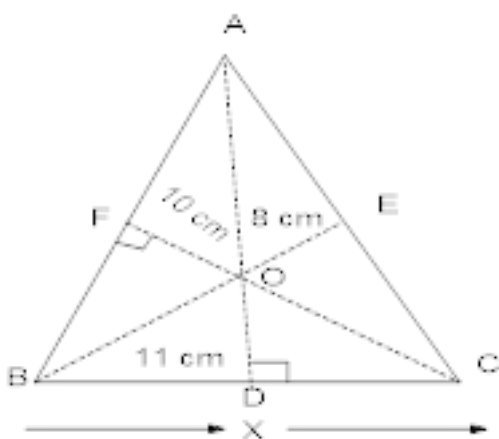
$$\Rightarrow BM = \frac{84 \times 2}{15} = 11.2 \text{ m}$$

Now area of trapezium ABCD = $\frac{1}{2}(AB + CD) \times BM$

$$= \frac{1}{2}(10 + 25) \times 11.2$$

$$= 196 \text{ m}^2$$

8. From a point in the interior of an equilateral triangle perpendiculars drawn to the three sides are 8 cm, 10 cm and 11 cm respectively. Find the area of the triangle to the nearest cm. (use $\sqrt{3} = 1.73$)



Ans. Let each side of the equilateral $\triangle ABC$ measure be x cm.

Let $OD = 11$ cm, $OE = 8$ cm and $OF = 10$ cm

Join OA , OB and OC

Now $ar(\triangle ABC) = ar(\triangle OBC) + ar(\triangle OCA) + ar(\triangle OAB)$

$$= \left(\frac{1}{2}x \times 11 + \frac{1}{2}x \times 8 + \frac{1}{2}x \times 10 \right) \text{Sq cm}$$

$$= \frac{29}{2}x \text{ sq cm} \rightarrow (1)$$

But area of equilateral \triangle , the measure of whose each side of x

$$= \frac{\sqrt{3}}{4} x^2 \text{ sq cm} \rightarrow (ii)$$

From (i) and (ii)

$$\frac{\sqrt{3}}{4} x^2 = \frac{29}{2}x$$

$$\therefore x = \frac{4 \times 29}{\sqrt{3} \times 2} = \frac{58}{\sqrt{3}}$$

$$\therefore \text{area of } \triangle ABC = \frac{29}{2} \times \frac{58}{\sqrt{3}} = \frac{841\sqrt{3}}{3} \text{ sq cm}$$

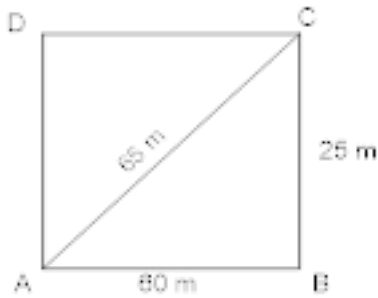
$$= \frac{841 \times 1.73}{3} = 485 \text{ sq cm}$$

9. A parallelogram, the length of whose side is 60 m and 25 m has one diagonal 65 m long. Find the area of the parallelogram.

Ans. $AB = DC = 60$ cm, $BC = AD = 25$ m and $AC = 65$ m

Area of parallelogram ABCD = Area of $\triangle ABC$ + area of $\triangle ACD$

= 2 Area of $\triangle ABC$ [\therefore ar $\triangle ABC$ = ar $\triangle ABD$]



Now

$$S = \frac{60 + 65 + 25}{2} m = 75m$$

$$\therefore \text{area of } \triangle ABC = \sqrt{S(s-a)(s-b)(s-c)}$$

$$= \sqrt{75(75-60)(75-65)(75-25)} \text{ sq m}$$

$$= (5 \times 3 \times 5 \times 2 \times 5) \text{ sq m}$$

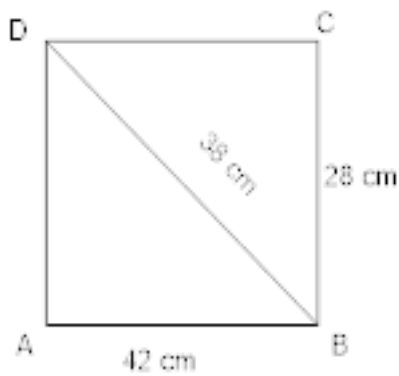
$$= 750 \text{ sq m} \dots \text{(II)}$$

From (i) and (ii), we get

Area of

$$11^{\text{th}} \text{ ABCD} = 2 \times 750 = 15000 \text{ sq m.}$$

10. A parallelogram, the measures of whose adjacent sides are 28 cm and 42 cm, has one diagonals 38cm. Find Its altitude on the side 42cm.



Ans. $AB=DC=42\text{cm}=c$

$BC=AD= 28\text{cm} =b$

And $BD=38\text{cm}=a$

Let A be the area of $\triangle ABD$

$$\text{Now, } S = \frac{38 + 28 + 42}{2} = 54\text{cm}$$

$$A = \sqrt{54(54 - 38)(54 - 28)(54 - 42)}$$

$$= \sqrt{54 \times 16 \times 26 \times 12} \text{ sq cm .}$$

$$= 144\sqrt{13} \text{ sq cm}$$

\therefore area of $\triangle ABD$

$$\text{again area of } \triangle ABD = \frac{1}{2} \text{base} \times \text{altitude}$$

$$= \frac{1}{2} \times 42 \times h \text{ sq cm, where } h \text{ cm is altitude}$$

$$= 21h \text{ sq cm}$$

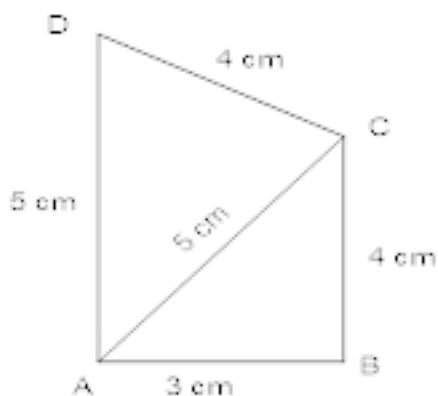
From (i) and (ii), we get

$$21h = 144\sqrt{13}$$

$$h = \frac{144\sqrt{13}}{21} = \frac{48\sqrt{13}}{7} \text{ cm}$$

Thus, required altitude = $\frac{48\sqrt{13}}{7} \text{ cm}$

12. Find the area of a quadrilateral ABCD in which AB=3 cm, BC=4 cm, CD= 4 cm, DA=5cm and AC= 5 cm.



Ans. \therefore Area of quadrilateral ABC=area of $\triangle ABC$ + area of $\triangle ACD$ (i)

For $\triangle ABC$, $S = \frac{3+4+5}{2} = 6 \text{ cm}$

\therefore Area of $\triangle ABC = \sqrt{6(6-3)(6-4)(6-5)}$
 $= \sqrt{6 \times 3 \times 2 \times 1} \text{ sq cm} = 6 \text{ sq cm} \dots(i)$

For $\triangle ACD$, $S = \frac{5+4+5}{2} = 7 \text{ cm}$

\therefore area of $\triangle ACD$

13. Find the base of an isosceles triangles whose area is 12cm and the length of one of the equal side is 5cm.

Ans. \therefore Area of an isosceles triangle = $\frac{a}{4} \sqrt{4b^2 - a^2}$

$$\therefore \frac{a}{4} \sqrt{4b^2 - a^2} = 12$$

$$\text{or } \frac{a}{4} \sqrt{100 - a^2} = 12$$

Squaring both sides, we have

$$a^2(100 - a^2) = 144 \times 16$$

$$= 2304$$

$$\text{or } a^4 - 100a^2 + 2304 = 0$$

$$\text{or } (a^2 - 64)(a^2 - 36) = 0$$

$$\therefore \text{Either } a^2 = 64 \text{ i.e. } a = \pm 8$$

$$\text{or } a^2 = 36 \text{ i.e. } a = \pm 6$$

$$\therefore \text{Required base} = 8 \text{ cm or } 6 \text{ cm}$$

14. The perimeter of a triangle is 450m and its sides are in the ratio of 13:12:5. Find the area of the triangle.

Ans. Let the sides of the triangle be $13x$, $12x$ and $5x$

Perimeter of a triangle = 450 m

$$\therefore 13x + 12x + 5x = 450 \text{ m}$$

$$\text{or } 30x = 450$$

$$\therefore x = 15$$

$$\therefore \text{The sides are } 13 \times 15, 12 \times 15, \text{ and } 5 \times 15$$



I.e. 195 m, 180 m and 75 m

$$\therefore S = \frac{a+b+c}{2} = \frac{450}{2} = 225 \text{ m}$$

$$\therefore \text{Area of the triangle} = \sqrt{s(s-a)(s-b)(s-c)} \text{ sq m}$$

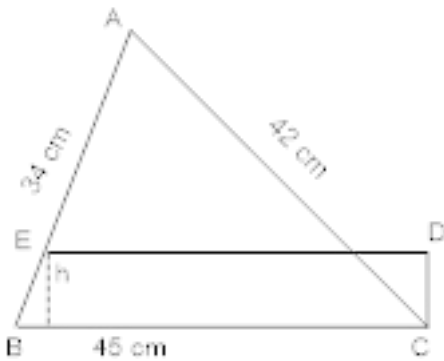
$$= \sqrt{225(225-195)(225-180)(225-75)} \text{ sq m}$$

$$= \sqrt{225 \times 30 \times 45 \times 150} \text{ sq m}$$

$$= (15 \times 15 \times 2 \times 3 \times 5) \text{ sq m}$$

$$= 6750 \text{ sq m.}$$

15. The sides of a triangle are 39cm, 42cm and 45cm. A parallelogram stands on the greatest side of the triangle and has the same area as that of the triangle. Find the height of the parallelogram.



Ans. To find the area of $\triangle ABC$

$$S = \frac{45+42+39}{2} \text{ cm}$$

$$= 63 \text{ cm}$$

$$\therefore \text{Area of } \triangle ABC = \sqrt{63(63-45)(63-42)(63-39)} \text{ sq cm}$$

$$= \sqrt{63 \times 18 \times 21 \times 24} \text{ sq cm}$$

$$= 9 \times 7 \times 2 \times 3 \times 2 \text{ sq cm}$$

$$= 756 \text{ sq cm}$$

Let h be the height of the parallelogram

Now,

Area of parallelogram BCDE = Area of $\triangle ABC$

$$\therefore h \times BC = 756$$

$$\text{or } 45h = 756$$

$$h = \frac{756}{45}$$

$$h = 16.8 \text{ cm}$$

Hence, height of the parallelogram = 16.8 cm

16. The students of a school staged a rally for cleanliness campaign. They walked through the lanes in two groups. One group walked through the lanes AB, BC and CA while the other group through the lanes AC, CD and DA [fig1.1]. Then they cleaned the area enclosed within their lanes. If $AB=9\text{m}$, $BC=40\text{m}$, $CD=15\text{m}$, $DA=28\text{m}$ and $\angle B=90^\circ$, which group cleaned more area and by how much? Find also the total area cleaned by the students.

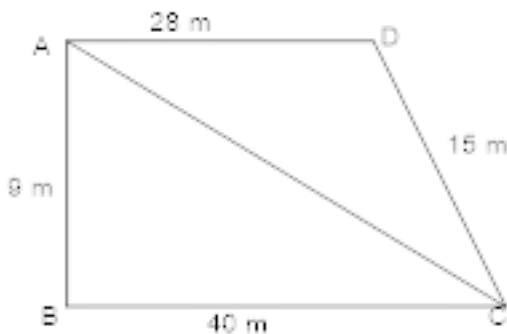


Fig. 1.1

Ans. We have, right angle $\triangle ABC$,



$$AC^2 = AB^2 + BC^2$$

$$AC^2 = 9^2 + 40^2$$

$$AC^2 = 1681$$

$$\therefore AC = 41$$

The first group has to clean the area of $\triangle ABC$ which is right angled triangle

Now,

$$\text{Area of } \triangle ABC = \frac{1}{2} \times 40 \text{ m} \times 9 \text{ m}$$

$$= 180 \text{ sq m}$$

The second group has to clean the area of $\triangle ACD$ which has $AD=28$ m,

$DC=15$ m and $AC=41$

Hence,

$$S = \frac{28+15+41}{2}$$

$$= 42 \text{ m}$$

$$\therefore \text{Area of } \triangle ACD = \sqrt{42(42-28)(42-15)(42-41)} \text{ sq m}$$

$$= \sqrt{42 \times 14 \times 27 \times 1} \text{ sq m}$$

$$= \sqrt{7 \times 3 \times 2 \times 7 \times 2 \times 9 \times 3} \text{ sq m}$$

$$= 126 \text{ sq m}$$

$$\therefore \text{First group cleaned more} = (180 - 126) \text{ sq m}$$

$$= 54 \text{ sq m}$$

∴ Total area cleaned by students = (180 + 126) sq m

= 306 sq m

17. A traffic signal board indicating 'school ahead' is an equilateral triangle with side 'a' find the area of the signal board using heron's. Its perimeter is 180 cm, what will be Its area?

Ans. $S = \frac{a+a+a}{2}$ units = $\frac{3a}{2}$ units

∴ Area of triangle = $\sqrt{\frac{3a}{2} \times (\frac{3a}{2} - a)(\frac{3a}{2} - a)(\frac{3a}{2} - a)}$

= $\sqrt{\frac{3a}{2} \times \frac{a}{2} \times \frac{a}{2} \times \frac{a}{2}}$

= $\frac{a^2}{4} \sqrt{3}$ sq units

Now, perimeter = 180 cm

∴ each side = $\frac{180}{3} = 60$ cm

∴ Area of signal board = $\frac{\sqrt{3}}{4} (60)^2$ sq cm

= $900 \sqrt{3}$ sq cm

18. A parallelogram the length of whose sides are 80m, and 40m has one diagonal 75m long. Find the area of the parallelogram?

Ans. $AB = DC = 80$ cm

$BC = AD = 40$ cm and $AC = 75$ cm

$$\text{In } \triangle ABC, S = \frac{80 + 40 + 75}{2} = 97.5 \text{ cm}$$

$$\begin{aligned}\text{Area of triangle ABC} &= \sqrt{s(s-a)(s-b)(s-c)} \\ &= \sqrt{97.5(97.5-80)(97.5-40)(97.5-75)} \text{ sq m} \\ &= \sqrt{97.5 \times 17.5 \times 57.5 \times 22.5} \text{ sq m} \\ &= \sqrt{2207460.94}\end{aligned}$$

$$= 1485.75 \text{ sq m}$$

$$\text{Area of parallelogram ABCD} = 2 \times \text{Area of } \triangle ABC$$

$$= 2 \times 1485.7$$

$$= 2971.4 \text{ sq m}$$

19. The side of a triangular field is 52m, 56m, and 60m find the cost of leveling the field Rs 18 per meter, if a space of 4cm is to be left for entry gate.

Ans. Side of the field are 52m, 56m and 60m.

$$\therefore S = \frac{52 + 56 + 60}{2} = 84 \text{ m}$$

$$\therefore \text{Area of field} = \sqrt{84(84-52)(84-56)(84-60)} \text{ Sq m}$$

$$= \sqrt{(7 \times 12)(2 \times 16)(4 \times 7)(12 \times 2)} \text{ sq m}$$

$$= \sqrt{7 \times 7 \times 12 \times 12 \times 2 \times 2 \times 4 \times 16} \text{ sq m}$$

$$= 1344 \text{ sq m}$$

$$\therefore \text{Total cost of levelling the field} = \text{Rs } 18 \times 1344$$

$$= \text{Rs } 24192$$



20. A floral design of a floor is made up of 16 tiles which are triangular. The side of the triangle being 9 cm, 28 cm, and 35 cm. find the cost of polishing the tiles, at RS 50 paisa/sq cm.

Ans. For each triangular tile, we have

$$S = \frac{35 + 28 + 9}{2} \text{ cm} = 36 \text{ cm}$$

$$\therefore \text{Area of Each tile} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{36(36-35)(36-28)(36-9)} \text{ sq cm}$$

$$= 36\sqrt{6} \text{ sq cm}$$

$$\therefore \text{Area of 16 tile} = 16 \times 36\sqrt{6} \text{ sq cm}$$

$$\therefore \text{cost of polishing} = \text{Rs} \left[\frac{1}{2} \times 16 \times 36\sqrt{6} \right] = \text{Rs} 288\sqrt{6}$$

$$= \text{Rs}(288 \times 2.45) = \text{Rs} 705.60$$

21. The measure of one side of a right triangle is 42m. If the difference in lengths of Its hypotenuse and other side is 14 cm, find the measure of two unknown side?

Ans. Let AB = y and AC = x and BC = 42 cm

\therefore By the given condition,

$$x - y = 14 \text{ (i)}$$

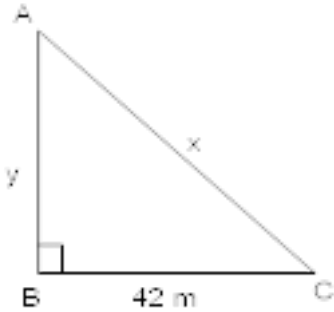
By Pythagoras theorem,

$$x^2 - y^2 = 1764$$

$$(x + y)(x - y) = 1764$$

$$\therefore 14(x + y) = 1764 \text{ using (ii)}$$

$$\therefore x + y = \frac{1764}{14} = 126 \text{ (iii)}$$



Adding (ii) and (iii), we get

$$2x = 140$$

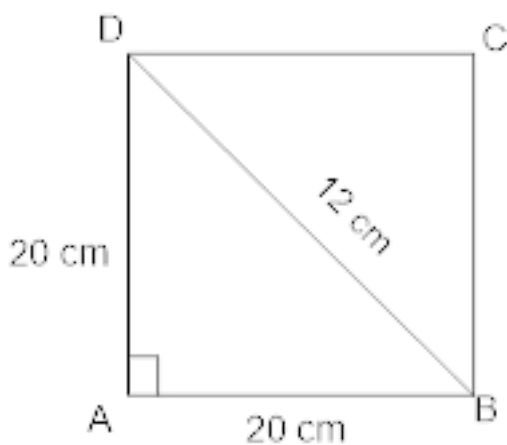
$$\text{i.e. } x = 70$$

$$\therefore y = 126 - x$$

$$y = 126 - 70$$

$$= 56$$

22. The perimeter of a rhombus ABCD is 80 cm. find the area of rhombus if Its diagonal BD measures 12 cm.



Ans. $\therefore AB = BC = CD = DA = \frac{80}{4} = 20 \text{ cm}$

Now in $\triangle ABD$,

$$\therefore S = \frac{20+20+12}{2} = 26$$

so,

$$\text{Area of } \triangle ABD = \sqrt{26 \times 6 \times 6 \times 14} \text{ sq cm}$$

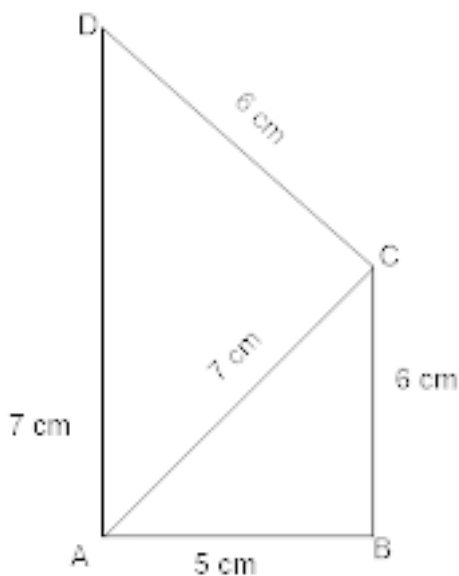
$$= 114.4 \text{ sq cm}$$

$$\text{Area of rhombus} = 2 \times \text{area of } \triangle ABD$$

$$= 2 \times 114.4 \text{ sq cm}$$

$$= 228.8 \text{ sq cm}$$

23. Find area of quadrilateral ABCD in which AB= 5 cm, BC= 6 cm, CD 6 cm, DA =7cm, And AC=7 cm.



Ans. Area of quadrilateral ABCD = Area of $\triangle ABC$ + Area of $\triangle ACD$ (i)

In $\triangle ABC$,

$$S = \frac{5+6+7}{2} = 9 \text{ cm}$$

$$\therefore \text{Area of } \triangle ABC = \sqrt{9(9-5)(9-6)(9-7)} \text{ sq cm}$$

$$= \sqrt{9 \times 4 \times 3 \times 2} \text{ sq cm}$$

$$= 6\sqrt{6} \text{ sq cm} = 14.4 \text{ sq cm}$$

In $\triangle ACD$,

$$S = \frac{7+7+6}{2} = 10 \text{ cm}$$

$$\therefore \text{Area of } \triangle ACD = \sqrt{10(10-7)(10-7)(10-6)} \text{ sq cm}$$

$$= \sqrt{10 \times 3 \times 3 \times 4} \text{ sq cm}$$

$$= 18.9 \text{ sq cm}$$

$$\text{Area of quadrilateral ABCD} = (14.4 + 18.9) \text{ sq cm}$$

$$= 33.3 \text{ sq cm.}$$

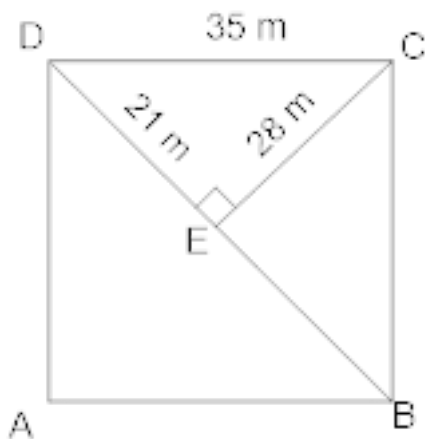
24. Shashi Kant has a vegetable garden in the shape of a rhombus. The length of each side of garden is 35 m And Its diagonal is 42 m long. After growing the vegetables in it. He wants to divide it in seven equal parts And look after each part once a week. Find the area of the garden which he has to look after daily.

Ans. Let ABCD be garden

$$\therefore DC = 35 \text{ m} \dots \dots \text{ (Given)}$$

$$DB = 42 \text{ m} \dots \dots \text{ (Given)}$$

Draw $CE \perp DB$



We know that the diagonals of a rhombus bisect each other at right angles.

$$\therefore DE = \frac{1}{2} DB = \frac{1}{2} \times 42 \quad \text{or } 21 \text{ m}$$

Now

$$CE^2 = CD^2 - DE^2$$

$$= 35^2 - 21^2$$

$$= 784$$

$$CE = 28 \text{ m}$$

$$\text{Now area of } \triangle DBC, = \frac{1}{2} \times DB \times CE$$

$$= \frac{1}{2} \times 42 \times 28$$

$$= 588 \text{ sq m}$$

$$\therefore \text{Area of the garden ABCD} = 2 \times 588 \text{ sq m}$$

$$= 1176 \text{ sq m}$$

Area of the garden he has to look after, daily

$$= \frac{1176}{7} \text{ sq m}$$

$$= 168 \text{ sq m}$$

25. The perimeter of a triangle is 480 meters and its sides are in the ratio of 1:2:3. Find the area of triangle?

Ans. Let the sides of the triangle be x , $2x$, $3x$

Perimeter of the triangle = 480 m

$$\therefore x + 2x + 3x = 480 \text{ m}$$

$$6x = 480 \text{ m}$$

$$x = 80 \text{ m}$$

\therefore The sides are 80 m, 160 m, 240 m

So,

$$S = \frac{80 + 160 + 240}{2} = \frac{480}{2}$$
$$= 240 \text{ m}$$

And,

$$\therefore \text{Area of triangle} = \sqrt{s(s-a)(s-b)(s-c)} \text{ sq m}$$

$$= \sqrt{240(240-80)(240-160)(240-240)} \text{ sq m}$$

$$= 0 \text{ sq m}$$

\therefore Triangle doesn't exist with the ratio 1:2:3 whose perimeter is 480 m.

26. Find the cost of leveling the ground in the form of equilateral triangle whose side is 12 m at Rs 5 per square meter.



Ans. Here, sides are 12 m, 12 m, 12 m,

$$\therefore S = \frac{12+12+12}{2}$$

$$= 18 \text{ cm}$$

And,

$$\therefore \text{Area of equilateral triangle} = \sqrt{s(s-a)(s-b)(s-c)} \text{ sq m}$$

$$= \sqrt{18(18-12)(18-12)(18-12)} \text{ sq m}$$

$$= \sqrt{18 \times 6 \times 6 \times 6} \text{ sq m}$$

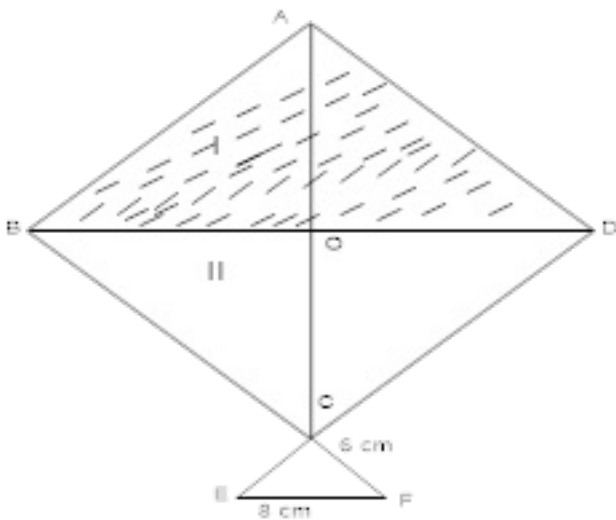
$$= \sqrt{6 \times 3 \times 6 \times 6 \times 6} \text{ sq m}$$

$$= 36\sqrt{3} \text{ sq m}$$

$$\therefore \text{Cost of leveling ground} = \text{Rs } (5 \times 36 \times 1.73)$$

$$= \text{Rs } 311.4 \text{ m}$$

27. A kite in the shape of a square with diagonal 32 cm and an isosceles triangle of base 8 cm and side 6 cm each is to be made of three different shades. How much paper of each shade has been used in it? (use $\sqrt{5} = 2.24$)



Ans. Let ABCD be the square and $\triangle CEF$ be an isosceles triangle.

Let the diagonals bisect each other at O.

Then,

$$AO = \frac{1}{2} \times 32 \text{ cm}$$

$$= 16 \text{ cm}$$

$$\text{Area of shaded portion I} = \frac{1}{2} \times 16 \times 32 \text{ sq cm}$$

$$= 256 \text{ sq cm}$$

And,

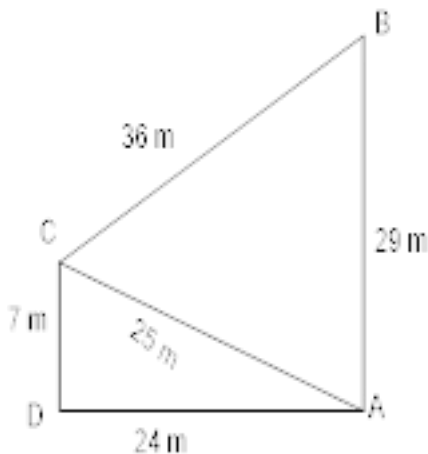
$$\text{Area of portion III} = \frac{a}{4} \sqrt{4b^2 - a^2}$$

$$= \frac{8}{4} \sqrt{4 \times (6)^2 - 8}$$

$$= 17.92 \text{ sq cm}$$

Thus, the papers of three shades required are 256 sq cm, 256 sq cm and 17.92 sq cm.

28. The sides of a quadrangular field, taken in order are 29 m, 36 m, 7m and 24 m respectively. The angle contained by the last two sides is a right angle. Find its area.



Ans. In $\triangle ADC$, which are right angles?

$$\therefore AC^2 = AD^2 + DC^2$$

$$= (24)^2 + (7)^2$$

$$= 576+49=625$$

$$\therefore AC = \sqrt{625} = 25$$

Area of quad ABCD = Area of $\triangle ADC$ + Area of $\triangle ABC \rightarrow$ (I)

$$\text{Area of } \triangle ADC = \frac{1}{2} AD \times CD = \frac{1}{2} \times 24 \times 7 \text{ sq m}$$

$$= 84 \text{ sq m} \rightarrow \text{(II)}$$

For $\triangle ABC$,

$$\therefore S = \frac{36 + 25 + 29}{2} M = 45M$$

$$\therefore \text{Area of } \triangle ABC, = \sqrt{45(45-36)(45-25)(45-29)}$$
$$= 360 \text{ sq m} \rightarrow \text{(III)}$$

From (I), (II) and (III) we get area of quadrilateral ABCD = (84+360) sq m = 444 sq m

29. Find the area of a triangle whose perimeter is 180 cm and two of its sides are 80 cm and 18 cm. hence calculate the altitude of the triangle taking the longest side as base.

Ans. Let a = 80 cm and b = 18 cm, perimeter = 180 cm

$$\therefore 180 = a + b + c = 80 + 18 + c$$

$$c = 82 \text{ cm}$$

$$\text{Now, } S = \frac{180}{2} = 90 \text{ cm}$$

$$\therefore \text{Area of triangle} = \sqrt{90(90-80)(90-18)(90-82)}$$

$$= \sqrt{90 \times 10 \times 72 \times 8} \text{ sq cm}$$

$$= 720 \text{ sq cm}$$

The longest side of triangle is 82 cm

Let h cm be length of altitude corresponding to longest side.

CBSE Class 9 Mathemaics

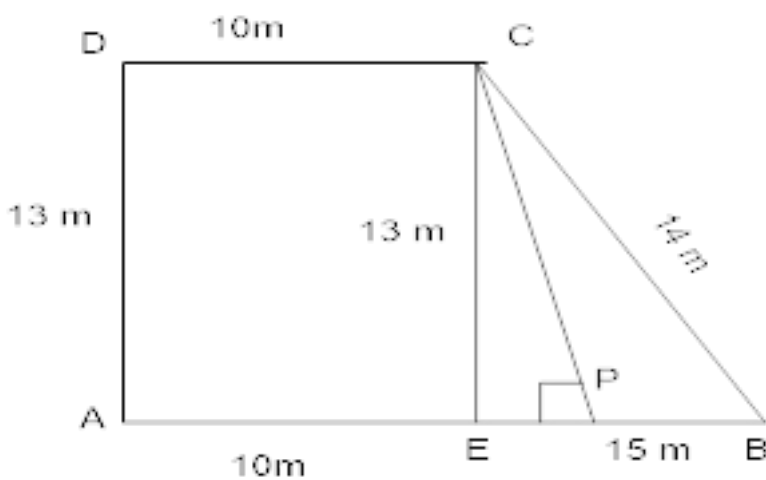
Important Questions

Chapter 12

Hérons Formula

4 Marks Quetions

1. A field in the shape of a trapezium whose parallel side are 25m and 10m. The non-parallel side are 14 m and 13 m. Find the area of the field.



Ans. AB=25m, CD =10m

AD=13m and BC=14

Draw $EC \parallel AD$ and $CP \perp EB$

Now $CE = AD = 13m$ and

$EB = AB - AE = (25 - 10) m = 15m$

In $\triangle BCE$, $a = 15m$, $b = 14m$ and $c = 13m$

$$\therefore S = \frac{a+b+c}{2} = \frac{15+14+13}{2}$$

=21 m

$$\therefore \text{area of } \triangle BCE = \sqrt{21(21-15)(21-14)(21-13)}$$

$$= \sqrt{21 \times 6 \times 7 \times 8} \text{ sq m}$$

$$= 84 \text{ sq m(i)}$$

$$\text{Also area of } \triangle BCE = \frac{1}{2} \times BE \times CP$$

$$CP = \frac{2 \text{area of } \triangle BCE}{BE} = \frac{2 \times 84}{15} \text{ m} = \frac{56}{5} \text{ m [using (i)]}$$

Now, area of parallelogram AECD = Base \times height

$$= 10 \times \frac{56}{5} \text{ m} = 112 \text{ sq m(ii)}$$

Thus area of trapezium ABCD = area of parallelogram + area of $\triangle BCE$

$$= 112 \text{ sq m} + 84 \text{ sq m [using (i) and (ii)]}$$

$$= 196 \text{ sq m}$$

2. The perimeter of a right triangle is 24 cm. If its hypotenuse is 10 cm, find the other two sides. Find its area by using the formula area of a right triangle. Verify your result by using Heron's formula.

Ans. Let x and y be the two lines of the right \angle .

$$\therefore AB = x \text{ cm, } BC = y \text{ cm and } AC = 10 \text{ cm}$$

\therefore By the given condition,

$$\text{Perimeter} = 24 \text{ cm}$$

$$\text{Or } x + y = 14 \text{ (1)}$$

By Pythagoras theorem,



$$x^2 + y^2 = (10)^2$$

$$= 100 \text{ (2)}$$

$$\text{From (1), } (x + y)^2 = (14)^2$$

$$\text{Or } x^2 + y^2 + 2xy = 196$$

$$\therefore 100 + 2xy = 196 \text{ from (2)}$$

$$xy = \frac{96}{2}$$

$$= 48 \text{ sq cm (3)}$$

$$\text{Area of } \triangle ABC = \frac{1}{2} xy \text{ sq cm}$$

$$= \frac{1}{2} \times 48 \text{ sq cm}$$

$$= 24 \text{ sq cm (4)}$$

again,

$$(x - y)^2 = (x + y)^2 - 4xy$$

$$= (14)^2 - 4 \times 48$$

$$\text{Or } x - y = \pm 2$$

(i) When, $x - y = 2$ and $x + y = 14$, then $2x = 16$

$$\text{or } x = 8, y = 6$$

(ii) When, $x - y = -2$ and $x + y = 14$, then $2x = 12$

$$\text{Or } x = 6, y = 8$$

Verification by using Heron's formula:

Sides are 6 cm, 8 cm and 10 cm

$$S = \frac{24}{2} = 12 \text{ cm}$$

$$\text{Area of } \triangle ABC = \sqrt{12(12-6)(12-8)(12-10)} \text{ sq cm}$$

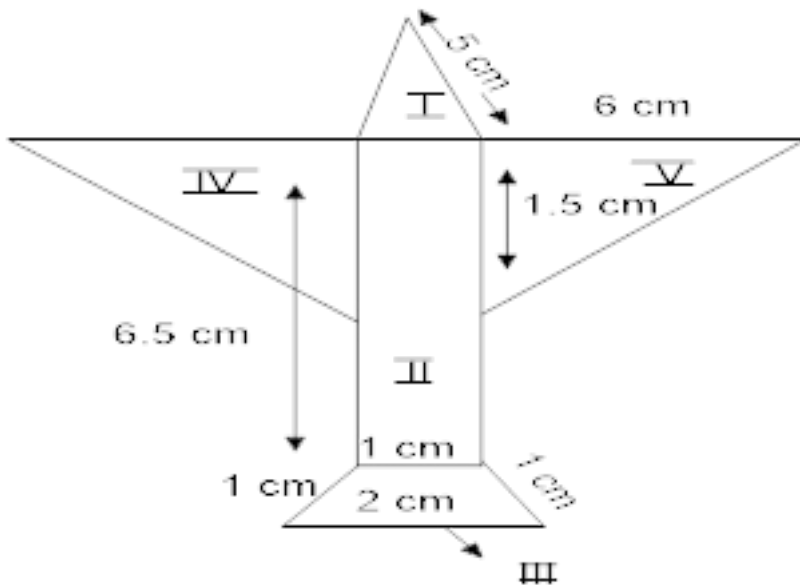
$$= \sqrt{12 \times 6 \times 4 \times 2} \text{ sq cm}$$

$$= 24 \text{ sq cm}$$

Which is same as found in (4)

Thus, the result is verified.

3. Radha made a picture of an aero plane with colored paper as shown in fig. find the total area of the paper used.



Ans. Area (1) = area of isosceles triangle with a = 1 cm and b = 5 cm

$$= \frac{a}{4} \sqrt{4b^2 - a^2}$$

$$= \frac{1}{4} \sqrt{100-1} = \frac{\sqrt{99}}{4} \text{ sq cm (approx)}$$

Area (ii) = area of rectangle with

$$L = 6.5 \text{ cm and } b=1 \text{ cm}$$

$$= 6.5 \times 1 \text{ sq cm} = 6.5 \text{ sq cm}$$

Area (iii) = Area of trapezium

$$= 3 \times \text{Area of equilateral } \Delta \text{ with side} = 1 \text{ cm}$$

$$= 3 \times \frac{\sqrt{3}}{4} \times (1)^2 \text{ sq cm}$$

$$= \frac{3 \times 1.732}{4} \text{ or } \frac{5.196}{4} \text{ sq cm}$$

$$= 1.3 \text{ sq cm (approx.)}$$

$$\text{Area of (IV + V)} = 2 \times \frac{1}{2} \times 6 \times 1.5 \text{ sq cm} = 9 \text{ sq cm}$$

\therefore total area of the paper used = Area (I+II+III+IV+V)

$$= (2.5+6.5+1.3+9) \text{ sq cm}$$

$$= 19.3 \text{ sq cm}$$

